

#### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
  - there may be more space than you need.

#### Information

- The total mark for this paper is 120.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.
- In questions marked with an **asterisk** (\*), marks will be awarded for your ability to structure your answer logically, showing how the points that you make are related or follow on from each other where appropriate.
- The list of data, formulae and relationships is printed at the end of this booklet.

#### **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- You are advised to show your working in calculations including units where appropriate.

Turn over ▶

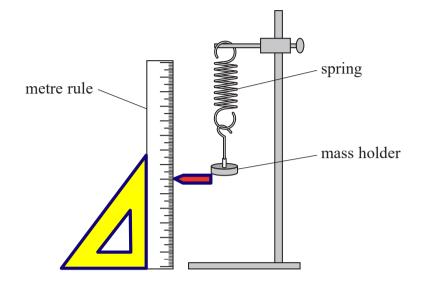






## Answer ALL questions in the spaces provided.

1 A student investigated the behaviour of a spring under tension. The spring was hung vertically with a mass holder attached, as shown. The position of the bottom of the mass holder was determined using a metre rule.



(a) The position of the bottom of the mass holder was recorded. The spring was stretched by adding masses to the mass holder and the new positions were determined. The extension of the spring for each mass was calculated.

The results are shown in the table.

Mass/kg	Extension/m
0.05	0.019
0.10	0.042
0.15	0.058
0.20	0.085
0.25	0.1
0.35	0.14

Criticise the recording of these results.

Extension not recorded to the same number of significant figures, and the position of the mass holder when no mass added was not recorded.



(b)	Describe how t	the student should	determine	the extension	of the	spring a	s accurate	ly
	as possible.							

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and	attack		a po	inter	- t	the	was.	Take	
repea	t re	adin	ez on	J	calcula	te o	L wear	./	vertical,

(Total for Question 1 = 5 marks)



- A student was given a box of identical glass microscope slides and asked to determine the density of the glass. She used a micrometer to measure the thickness of one of the slides. She repeated this measurement twice in different places and calculated a mean value for the thickness. The thickness of each slide was approximately 1 mm.
  - (a) Explain how she should have measured the thickness of the slides in order to minimise the percentage uncertainty.

Measure the thickness of a stack of slides and divide by the number of slides. The absolute uncertainty would have been the same, but with a lager measured value the perentage uncertainty would be

(b) In her report she wrote

"My value for the mass of the glass slides was precise, because I measured the mass using an electronic balance which was accurate to the nearest 0.01g. I reduced the effect of random error by repeating the measurement several times."

Comment on this statement.

Measuring to 0.01 g is the resolution of the instrument, whereas precision is related to the spread of multiple values. She is mistaken in her use of 'accuracy as this should relate to how close a value is to the true value. I she is correct about repeating and calculating a mean to reduce random error.

(Total for Question 2 = 6 marks)

3 It was suggested on an online forum that it would be possible to cook a chicken by repeatedly slapping the chicken with one hand.

It was claimed that the energy transferred to a chicken in 8000 slaps would be sufficient to raise the temperature of the chicken from 23 °C to 165 °C.

In an investigation to test the claim, the effective mass of the hand was taken as  $1.75 \,\mathrm{kg}$  and the speed of the hand just before impact with the chicken as  $6.25 \,\mathrm{m\,s^{-1}}$ .

(a) Deduce whether the data confirms that 8000 slaps would be sufficient. Assume that no energy is transferred from the chicken to the surroundings.

mass of chicken =  $0.875\,\mathrm{kg}$  specific heat capacity of chicken =  $1770\,\mathrm{J\,kg^{-1}\,K^{-1}}$  efficiency of energy transfer from the hand = 65%

 $E_{\tau} = \eta \times E_{k} \times n = 0.65 \times \frac{1}{2} m_{h} v^{2} \times 8000$ 

Et= 0.65 x 1 x1.75 x 6.25 x 8000 = 177,734.375 J

 $E = w_{c} = \frac{177,734.375}{0.875 \times 1770} = 114.8^{\circ}$ 

9= 0+ 00= 23+114.8 = 137.8

138°C< 165°C: not enough to cook it √

(b) Explain whether the assumption made in (a) is realistic.

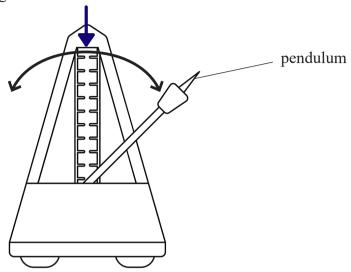
It is not realistic, as the chicken could not be insulated from the surroundings between slops so it wouldn't even get to 138°C.

(Total for Question 3 = 7 marks)



(5)

4 The diagram shows a metronome, which includes an inverted pendulum, used by musicians to set a tempo. The pendulum oscillates with simple harmonic motion and makes a loud click at regular intervals.



(Source: Getty Images)

A faulty metronome stopped making a clicking noise. A student tried to check the accuracy of the period T of the metronome, using a stopwatch. The student timed the pendulum as it moved from one extreme of the oscillation to the other.

Explain how the procedure used by the student to determine T could have been improved.

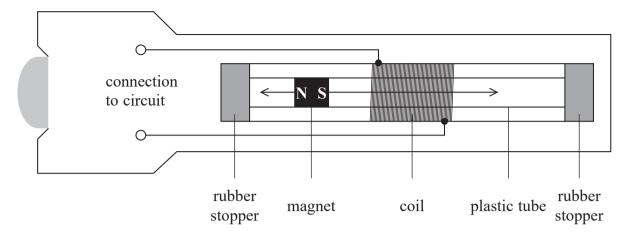
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(Total for Question 4 = 5 marks)

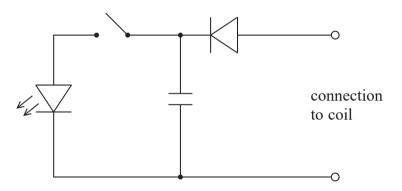
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\*5 The diagram shows a 'shaker torch'. When the torch is shaken, a strong magnet moves forwards and backwards through a copper coil, powering a light-emitting diode (LED).



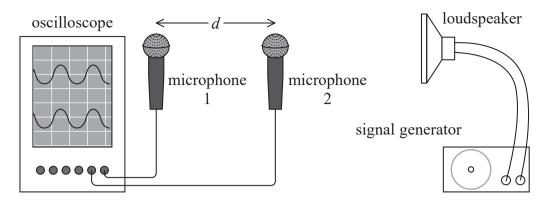
Each time the magnet moves through the coil a current pulse is generated. The coil is connected to a capacitor via a diode, as shown.



Once the torch has been shaken for a few minutes the switch is closed and the LED lights for a short while.

Explain how the shaker to	_		ومنا علم نو
a change in	ague mores magnetic H	ux linkage	coil there is √: an emp
is induced of	woss the	oil which	generates a
<b>1</b>	circuit Me		
current flar	in one dire	tion / .: cape	eitor gets
charged every	time the	tarch is	shaken.
When the	. suitch is	s closed,	the capacitor
is discharged	though -	the LED.	•
		(Total for Q	uestion 5 = 6 marks)

6 In an experiment to determine the speed of sound in air a student connected two microphones to an oscilloscope, as shown.



The microphones detect sound from the loudspeaker, converting it to an electrical signal. The signal is displayed on the oscilloscope screen.

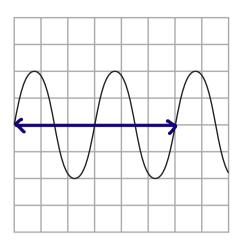
Both microphones were initially positioned the same distance from the loudspeaker. The two signals were in phase on the oscilloscope screen. The student slowly moved microphone 2 towards the loudspeaker, until the two signals on the oscilloscope were in phase again. He then measured the distance d between the microphones to determine the wavelength  $\lambda$  of the sound waves.

 $d = 20.5 \, \text{cm}$ 

(a) Comment on the student's experimental technique to determine  $\lambda$ .

Microphone 2 should have been wored further to the right to another position where the waves were in phase. This would have allowed the distance for multiple wavelengths to be measured, reducing percentage uncertainty.

(b) The oscilloscope trace for the signal from microphone 1 is shown below.



The time base of the oscilloscope was set to  $0.20\,\mathrm{ms}\,\mathrm{div}^{-1}$ .

Determine a value for the speed of sound in air.

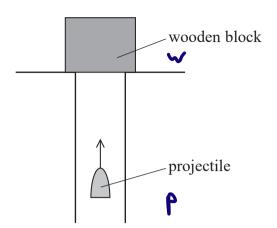
$$T = \frac{t}{n} = \frac{6.0 \times 0.20 \times 10^{-3}}{2.10} = 6.0 \times 10^{-4} \text{s}$$
 (5)

$$V = \int \lambda^{\frac{1}{2}} \frac{\lambda^{\frac{1}{2}}}{1} = \frac{0.205}{6.0 \times 10^{-4}} = 341.67$$

(Total for Question 6 = 7 marks)

**(6)** 

7 A projectile of mass 65 g is fired vertically upwards into a stationary wooden block of mass 2.400 kg, as shown.



(a) The projectile becomes embedded in the block. They both move vertically upwards through a vertical displacement of 55 cm before momentarily coming to rest.

Calculate the energy dissipated as the projectile hits the block.

After projectile embedded: Ex = Ep V

1/2 Mp Vp 2 = (Mw + Mp) g h

$$V_p = \sqrt{\frac{2(M_v + M_p)gh}{M_p}} = \sqrt{\frac{2(2.400 + 0.065) \times 1.81 \times 0.55}{0.065} = 3.285 \text{ m/s}^{-1}}$$

$$\frac{u_{p} = (u_{w} + u_{p}) \vee_{=} (2400 + 0.065) \times 3.285 = 124.576 \text{ ms}^{-1}}{u_{p}}$$

$$E_{\text{kindid}} = \frac{1}{2} w_{\text{p}} u_{\text{p}}^2 = \frac{1}{2} \times 0.065 \times 124.576^2 = 504.37 \text{ J/}$$

DE: 504.37-13.30: 491.07 J



(b) Explain how the principle of conservation of energy applies to this collision.

It is an inelastic collision, ar although manutum and total energy are conserved, the kinetic energy store decreases.

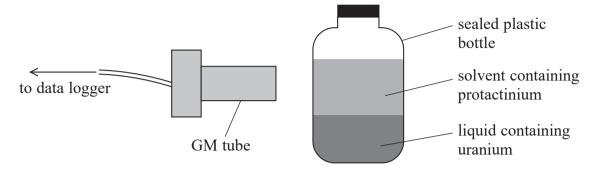
This is because the projectile does work an the block as it embeds, raising its internal energy.

(Total for Question 7 = 8 marks)

**(2)** 

**8** A teacher demonstrated the decay of protactinium using a Geiger-Müller (GM) tube connected to a data logger.

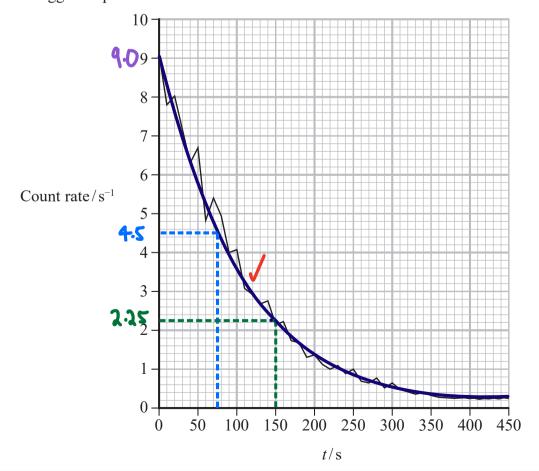
A sealed plastic bottle contains a solvent floating above a liquid containing a uranium salt. Protactinium is produced from the decay of uranium and is present in the solvent as shown.



(a) Deduce whether alpha radiation or beta radiation from the inside of the bottle is detected by the GM tube.

Alpha radiation would not penetrate the plantic bottle, so it went be beta as this can penetrate the plantic.

(b) The data logger output is shown below.



(i) Determine the half-life of the protactinium.

Activity starts at 9.0 st when t=0

2x+...  $2.25c^{-1}$  t = 150c

: ty = 75 s

Half-life of protactinium = 75 s

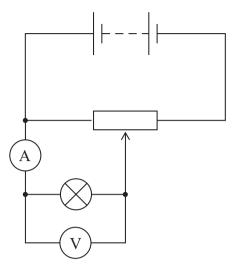
**(4)** 

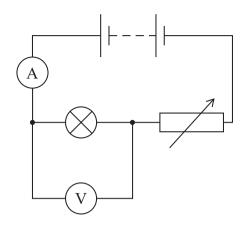
(ii) Explain why the count rate doesn't reach zero.

There will always be background radiation of detected by the GM tube and counted by the data bases.

(Total for Question 8 = 8 marks)

9 A student is planning to collect data to produce a current-potential difference graph for a filament lamp. Her teacher suggests two circuits that she could use.





Circuit 1

Circuit 2

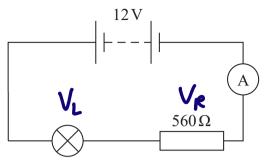
Circuit 1 uses a potential divider and circuit 2 uses a variable resistor to vary the potential difference across the filament lamp.

\*(a) Discuss the suitability of each circuit to collect the data.

Both circuits would work, at they allow readings of pd across, and current through, the lamp to be changed and measured. I win pd: OV/and max pd is the supply pd. I win pd > OV/and max pd is less than the supply pd, because the will always be a proportion of the pd across the variable resistor.

Circuit 1 allows a larger range of pds so is better.

(b) The student sets up the following circuit with the filament lamp. The battery has negligible internal resistance.



(i) The reading on the ammeter is 17.5 mA.

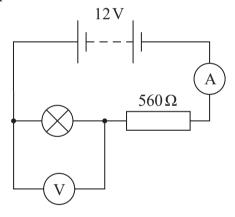
Calculate the value of the potential difference (p.d.) across the filament lamp.

$$V_{R} = [R = 17.5 \times 10^{-3} \times 560 = 9.8 \text{ V}]$$

$$V_{L} = V - V_{R} = 12 - 9.8 = 2.2$$

p.d. across filament lamp = 
$$2 \cdot 2 \sqrt{\phantom{a}}$$

(ii) When a voltmeter with a resistance of  $1.5\,\mathrm{k}\Omega$  is connected as shown, the p.d. across the filament lamp decreases.



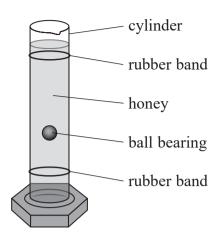
Explain why the p.d. across the filament lamp decreases.

The combined resistance of the lamp and voltanter is less than the resistance of just the lamp via a larger proportion of the supply pd is across this part of the circuit var this will be proportional to its share of the total resistance of the circuit.

(Total for Question 9 = 11 marks)



10 A student carried out an experiment to determine the viscosity of some honey. He filled a tall glass cylinder with honey as shown, and timed a ball bearing as it fell through the honey.



(a) The student placed rubber bands near the top and bottom of the cylinder. He started a stopwatch when the ball bearing passed the first band and stopped the stopwatch when the ball bearing passed the second band. He repeated this several times to determine a mean time.

Criticise the student's method.

The ball is unlikely to be at terminal velocity when it passes the first band, and the student wouldn't be able to check it is travelling at terminal velocity.

(b) The time t for the sphere to fall through a distance of 25.0 cm is shown in the table.

t/s					
6.40	6.35	6.36	6.38		

(i) Show that the mean velocity v of the ball bearing is about  $0.04\,\mathrm{m\,s^{-1}}$ .

$$V = \frac{5}{t} = \frac{0.250}{6.3725} = \frac{0.03923}{6.3725} \text{ ms}' \approx 0.04 \text{ ms}'$$

(ii) The student had three different types of honey available.

Viscosity  $\eta$  is given by the following expression

$$\eta = \frac{2r^2g\left(\rho_{\rm B} - \rho_{\rm H}\right)}{9v}$$

radius r of ball bearing =  $5.50 \times 10^{-3} \, \mathrm{m}$  density of ball bearing  $\rho_{\mathrm{B}} = 7750 \, \mathrm{kg \, m^{-3}}$  density of honey  $\rho_{\mathrm{H}} = 1360 \, \mathrm{kg \, m^{-3}}$ 

Viscosity (at 20°C)/Pas						
Honey A	Honey B	Honey C				
10.6	12.5	13.6				

Deduce which honey the student used.

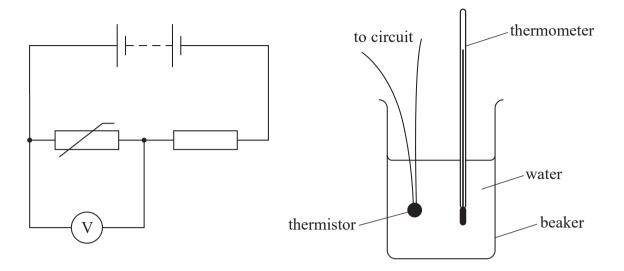
$$\eta = \frac{2 \times (5.50 \times 10^{-3})^2 \times 9.81 \times (7750 - 1360)}{9 \times 0.0392}$$

$$\eta = 10.74$$
 .: honey A

(Total for Question 10 = 7 marks)

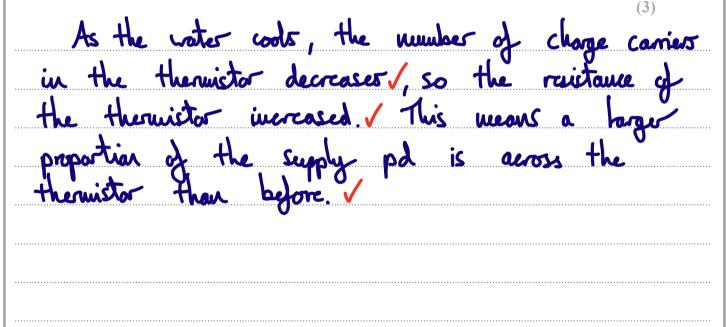


11 A student carried out an experiment to calibrate a thermistor. She connected the thermistor in series with a resistor and a power supply as shown. Then she placed the thermistor in a beaker of hot water and used a thermometer to record the temperature  $\theta$  of the water.



The student recorded  $\theta$  and corresponding values of the reading V on the voltmeter as the water cooled.

(a) Explain, making reference to charge carriers, why V increased as the water cooled.



(b) Over a limited temperature range V varies with  $\theta$  according to the expression

$$V = V_0 e^{-b\theta}$$

where b and  $V_0$  are constants.

(i) Explain why a graph of  $\ln V$  against  $\theta$  would give a straight line.

(2)

lu V= lu Vo - 60

luv=-60+ luvo / b= contant : equal to

y = wx+ c

a straight live.

(ii) The student's data is shown in the table below.

θ/°C	V/V	ln(V/V)
89.0	1.9	0.64
74.0	2.9	1.06
53.5	4.9	1.59
32.5	9.1	2.21
18.5	12.6	2.53
3.5	18.7	2.43 ✓

Plot a graph of  $\ln V$  against  $\theta$  on the grid opposite. Use the column provided to show any processed data.

**(5)** 

**(4)** 

(iii) Determine values for b and  $V_0$ .

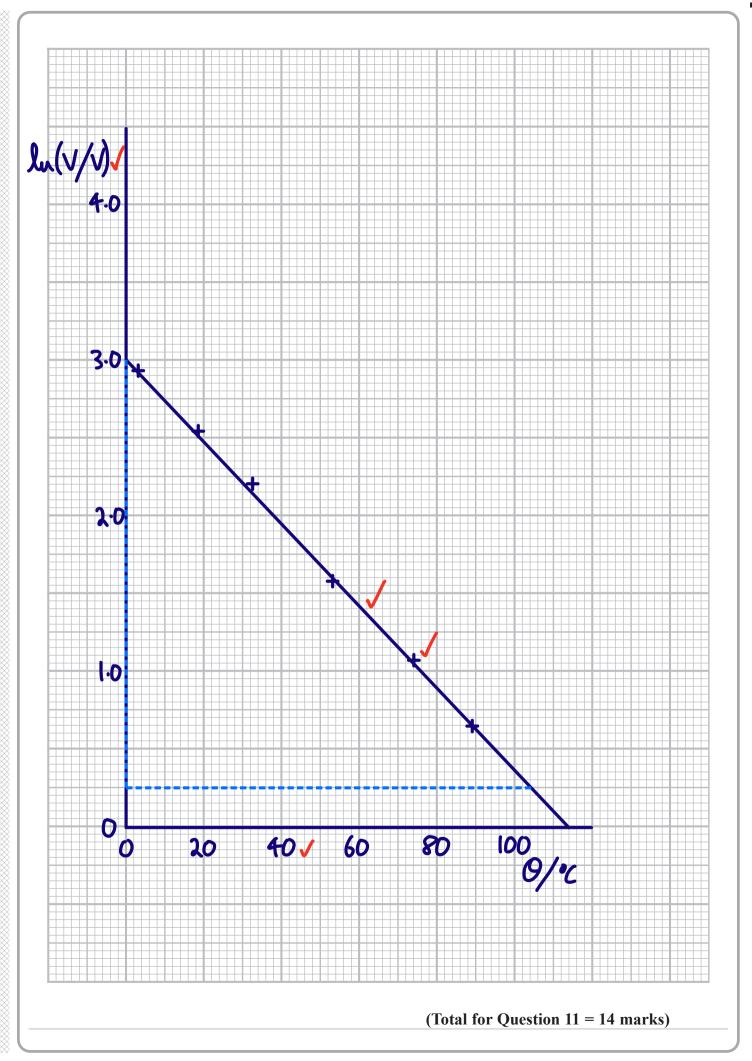
$$L_{11}V_{0}=3.0$$
  $V_{0}=e^{3.0}=20.086=20V$ 

 $b = -gradient = \frac{0.25 - 3.0}{104 - 0} = -0.0264 °C^{-1}$ 

$$b = \frac{0.026}{20 \text{ V}} \text{ C}^{-1} \text{ V}$$

$$V_0 = \frac{20 \text{ V}}{}$$







- 12 In 2011, a tsunami was caused by a massive earthquake centred some distance off the coast of Japan. The tsunami caused a cooling system failure at the Fukushima Nuclear Power Plant. This resulted in a nuclear meltdown and radioactive materials were released into the surroundings.
  - (a) A reservoir beside one of the reactor buildings contained a large volume of water. In 2013, this water was found to have an extremely high concentration of caesium-137.

Caesium-137 is a radioactive isotope of caesium.

(i) Complete the nuclear equation for the decay of caesium-137.

$$^{137}_{55}$$
Cs  $\rightarrow ^{137}_{56}$ Ba $^{\prime}+ ^{o}_{-1}\beta^{-}_{\checkmark}+ ^{0}_{0}\overline{\nu_{e}}$ 

(ii) An activity of  $2.35 \times 10^{12}$  Bq per m³ of water in the reservoir was measured. It is suggested that a safe level for the activity of all water in the reservoir would be 100 Bq.

Calculate the time in years for the caesium-137 to decay to a safe level.

volume of water in reservoir = 5000 m<sup>3</sup> half-life of caesium-137 = 30 years

$$t_{1/2} = \frac{\ln \lambda}{\lambda} \qquad \lambda = \frac{\ln \lambda}{\ln \lambda} = \frac{\ln \lambda}{30} = 0.0231 \text{ yr}^{-1} / \frac{1}{20}$$

$$A = A_0 e^{-\lambda t} / \ln \frac{A}{A_0} = -\lambda t \qquad t = \frac{\ln (A_0/A)}{\lambda}$$

$$t = \frac{\ln (2.35 \times 10^{12} \times 5000) / 100}{0.0231} = 1402$$

(b) The most common radionuclide amongst the fission products in the fuel was iodine-131, which decays with a half-life of 8.0 days to form a stable isotope of the gas xenon.

Deduce whether enough xenon would have collected in 32 days to exert a pressure of  $1.0 \times 10^5$  Pa in a volume of  $450 \,\mathrm{m}^3$ . Assume that no gas escapes.

temperature =  $20 \, ^{\circ}\text{C}$ initial number of iodine nuclei =  $1.25 \times 10^{28}$ 

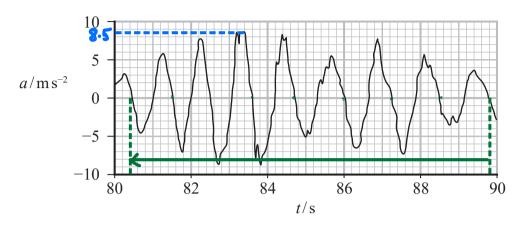
$$N = \frac{N_0}{2^n} = \frac{1.25 \times 10^{28}}{2^4} = 7.8125 \times 10^4$$
 (no. iodine lyt) \( \sqrt{}



**(6)** 

(c) Buildings in nearby Tohoku University suffered structural damage during the 2011 earthquake.

The graph shows how the acceleration of one of the buildings, measured on the 9th floor, varied with time during the earthquake.



(Source: https://www.sciencedirect.com/science/article/pii/S0038080612001035)

At the time it was reported that during the earthquake the 9th floor of the building displaced by more than 30 cm from its normal position.

Assess the accuracy of this report.

$$a_{\text{mex}} = 8.5 \text{ m/s}^{-2} / T = 89.8 - 80.4 = 1.175 s / 8$$

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{1.175} = 5.347 \text{ rod s}^{-1}/$$

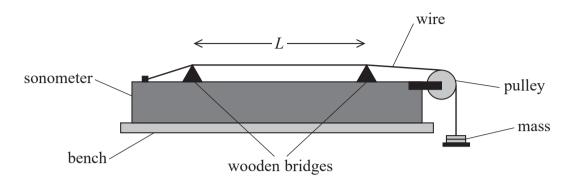
$$A_{\text{max}} = w^2 A$$

$$A = \frac{a_{\text{max}}}{w^2} = \frac{8.5}{5.347^2} = 0.297 \text{ m} \text{ } \checkmark$$

(Total for Question 12 = 17 marks)

13 A student used a sonometer to investigate the properties of a stretched wire. The sonometer is a long hollow wooden box.

A steel wire is attached to one end of the box and rests on two wooden bridges. The wire is placed under tension *T* by hanging a mass from the end of the wire, as shown.



The student placed the base of a vibrating tuning fork in contact with the wire, at one of the bridges. This set the wire into oscillation. He adjusted the position of the other bridge until a single-loop standing wave was produced on the wire between the bridges.

(a) Explain how an antinode is produced at the mid-point of the wire between the bridges.

Progressive	Laret	ar 1	offeited	from +	he opposite
bridge , when	n they	neet	in pha	le and	Superpose
constructive in	iter erwe	2 000	ws dim	ing mo	ximum
displacement /(	the an	tinode)		0	
	•	•			

(3)

(b) The student repeated this for a series of tuning forks with different frequencies f. For each fork he measured the distance L between the bridges.

The steel wire, of mass per unit length  $\mu$ , was placed under tension T by hanging a mass of 2.10 kg from the end of the wire.

(i) State one safety precaution that should be taken when carrying out the investigation.

(1)

(ii) The student plotted a graph of  $L^2$  against  $1/f^2$ .

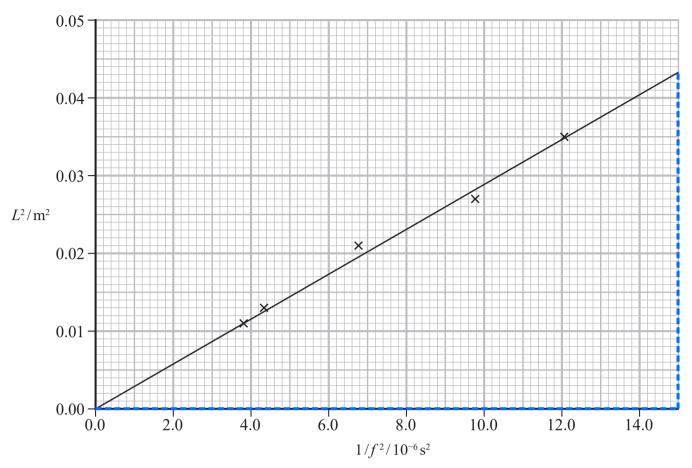
Show that the gradient of this graph is equal to  $\frac{T}{4\mu}$ 

(3)

v=fλ = 2fL√

$$L^{2} = \frac{1}{4\mu} \int_{-2}^{2}$$

(iii) The student's graph is shown below.



The value of  $\mu$  for different standard wire gauge (SWG) steel wire is shown in the table.

SWG	$\mu/\mathrm{g}\mathrm{m}^{-1}$
22	3.15
24	1.95
26	1.31

Deduce which wire the student used in the investigation.

gradient = 
$$\frac{0.43-0}{(15.0-0)\times10^{-6}} = 2.867\times10^{3} \text{ m}^{2}\text{ s}^{-2}$$

$$\frac{T}{4\mu} = \frac{2.867 \times 10^{3}}{4 \times 2.867 \times 10^{3}} = \frac{2.10 \times 9.81}{4 \times 2.867 \times 10^{3}} = \frac{2.10 \times 9.81}{4 \times 2.867 \times 10^{3}}$$

- (c) The student then found a value of  $\mu$  for a brass wire, using a different method.
  - (i) He measured the diameter d of the wire using a micrometer.

Explain one technique the student should use when measuring d.

Take readings in at least 3 different orientations along the wire in order to calculate the mean, as the wire man not be uniform.

30

(ii) The student obtained the following data.

d/mm						
0.55	0.59	0.57	0.58			

The stated value of  $\mu$  for the brass wire used by the student was  $2.14 \times 10^{-3} \,\mathrm{kg}\,\mathrm{m}^{-1}$ .

Deduce whether the student's data supports this value for  $\mu$ .

density of brass =  $8700 \, \text{kg} \, \text{m}^{-3} \pm 200 \, \text{kg} \, \text{m}^{-3}$ 

$$\frac{1}{\sqrt{100}} \times 100 = \frac{(0.59 - 0.55)/2}{(0.55 + 0.59 + 0.57 + 0.58)/4} \times 100 = 3.49\%$$

$$A = \frac{35\lambda^2}{4}$$
 :: %  $U_{\lambda} = 2 \times \% U_{\lambda} = 2 \times 3.49 = 6.987 \% \checkmark$ 

$$%U_{p} = \frac{200}{8700} \times 100 = 2.299 \% \checkmark$$

$$\mu = \frac{m}{L} = \frac{\rho V}{L} = \rho A \frac{k}{L} = \rho A$$

(Total for Question 13 = 19 marks)

TOTAL FOR PAPER = 120 MARKS



## List of data, formulae and relationships

Acceleration of free fall 
$$g = 9.81 \text{ m s}^{-2}$$
 (close to Earth's surface)

Boltzmann constant 
$$k = 1.38 \times 10^{-23} \text{ J K}^{-1}$$

Coulomb law constant 
$$k = \frac{1}{4\pi\varepsilon_0} = 8.99 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$

Electron charge 
$$e = -1.60 \times 10^{-19} \text{ C}$$

Electron mass 
$$m_a = 9.11 \times 10^{-31} \text{ kg}$$

Electronvolt 
$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$

Gravitational constant 
$$G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$$

Gravitational field strength 
$$g = 9.81 \text{ N kg}^{-1}$$
 (close to Earth's surface)

Permittivity of free space 
$$\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$$

Planck constant 
$$h = 6.63 \times 10^{-34} \text{ J s}$$

Proton mass 
$$m_{\rm p} = 1.67 \times 10^{-27} \text{ kg}$$

Speed of light in a vacuum 
$$c = 3.00 \times 10^8 \text{ m s}^{-1}$$

Stefan-Boltzmann constant 
$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

Unified atomic mass unit 
$$u = 1.66 \times 10^{-27} \text{ kg}$$

## Mechanics

Kinematic equations of motion

$$s = \frac{(u+v)t}{2}$$

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

Forces

$$\Sigma F = ma$$

$$g = \frac{F}{m}$$

$$W = mg$$

moment of force = Fx

Momentum

$$p = mv$$

Work, energy and power

$$\Delta W = F \Delta s$$

$$E_{k} = \frac{1}{2}mv^{2}$$

$$\Delta E_{\rm grav} = mg\Delta h$$

$$P = \frac{E}{t}$$

$$P = \frac{W}{t}$$

efficiency = 
$$\frac{\text{useful energy output}}{\text{total energy input}}$$

$$efficiency = \frac{useful power output}{total power input}$$



### **Electric circuits**

Potential difference

$$V = \frac{W}{Q}$$

Resistance

$$R = \frac{V}{I}$$

Electrical power and energy

$$P = VI$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$

$$W = VIt$$

Resistivity

$$R = \frac{\rho l}{A}$$

Current

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = nqvA$$

## **Materials**

Density

$$\rho = \frac{m}{V}$$

Stokes' law

$$F = 6\pi \eta r v$$

Hooke's law

$$\Delta F = k \Delta x$$

Young modulus

Stress 
$$\sigma = \frac{F}{A}$$

Strain 
$$\varepsilon = \frac{\Delta x}{x}$$

$$E = \frac{\sigma}{\varepsilon}$$

Elastic strain energy

$$\Delta E_{\rm el} = \frac{1}{2} F \Delta x$$

## Waves and particle nature of light

Wave speed

$$v = f\lambda$$

Speed of a transverse wave on a string

$$v = \sqrt{\frac{T}{\mu}}$$

Intensity of radiation

$$I = \frac{P}{A}$$

Power of a lens

$$P = \frac{1}{f}$$

$$P = P_{1} + P_{2} + P_{3} + \dots$$

Thin lens equation

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

Magnification for a lens

$$m = \frac{\text{image height}}{\text{object height}} = \frac{v}{u}$$

Diffraction grating

$$n\lambda = d \sin \theta$$

Refractive index

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$n = \frac{c}{v}$$

Critical angle

$$\sin C = \frac{1}{n}$$

Photon model

$$E = hf$$

Einstein's photoelectric equation

$$hf = \phi + \frac{1}{2}mv^2_{\text{max}}$$

de Broglie wavelength

$$\lambda = \frac{h}{p}$$



### **Further mechanics**

Impulse

$$F\Delta t = \Delta p$$

Kinetic energy of a non-relativistic particle

$$E_{k} = \frac{p^2}{2m}$$

Motion in a circle

$$v = \omega r$$

$$T = \frac{2\pi}{\omega}$$

$$F = ma = \frac{mv^2}{r}$$

$$a = \frac{v^2}{r}$$

$$a = r\omega^2$$

$$F = mr\omega^2$$

### **Fields**

Coulomb's law

$$F = \frac{Q_1 Q_2}{4\pi \varepsilon_0 r^2}$$

Electric field strength

$$E = \frac{F}{Q}$$

$$E = \frac{Q}{4\pi\varepsilon_0 r^2}$$

$$E = \frac{V}{d}$$

Electric potential

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

Capacitance

$$C = \frac{Q}{V}$$

Energy stored in a capacitor

$$W = \frac{1}{2}QV$$

$$W = \frac{1}{2}CV^2$$

$$W = \frac{1}{2} \frac{Q^2}{C}$$

Capacitor discharge

$$Q = Q_0 e^{-t/RC}$$

$$I = I_0 e^{-t/RC}$$

$$V = V_0 e^{-t/RC}$$

$$\ln Q = \ln Q_0 - \frac{t}{RC}$$

$$ln I = ln I_0 - \frac{t}{RC}$$

$$\ln V = \ln V_0 - \frac{t}{RC}$$

In a magnetic field

$$F = BIl \sin \theta$$

$$F = Bqv \sin \theta$$

Faraday's and Lenz's laws

$$\mathscr{E} = \frac{-\mathrm{d}(N\phi)}{\mathrm{d}t}$$

Root-mean-square values

$$V_{\rm rms} = \frac{V_0}{\sqrt{2}}$$

$$I_{\rm rms} = \frac{I_0}{\sqrt{2}}$$



## Nuclear and particle physics

In a magnetic field

$$r = \frac{p}{BQ}$$

## **Thermodynamics**

Heating

$$\Delta E = mc\Delta\theta$$

$$\Delta E = L\Delta m$$

Molecular kinetic theory

$$\frac{1}{2}m\langle c^2\rangle = \frac{3}{2}kT$$

$$pV = \frac{1}{3}Nm\langle c^2 \rangle$$

Ideal gas equation

$$pV = NkT$$

Stefan-Boltzmann law

$$L = \sigma A T^4$$

$$L = 4\pi r^2 \sigma T^4$$

Wien's law

$$\lambda_{\text{max}}T = 2.898 \times 10^{-3} \text{ m K}$$

#### **Space**

Intensity

$$I = \frac{L}{4\pi d^2}$$

Redshift of electromagnetic radiation

$$z = \frac{\Delta \lambda}{\lambda} \approx \frac{\Delta f}{f} \approx \frac{v}{c}$$

Cosmological expansion

$$v = H_0 d$$

# **Nuclear radiation**

Mass-energy

$$\Delta E = c^2 \Delta m$$

Radioactive decay

$$A = \lambda N$$

$$\frac{\mathrm{d}N}{\mathrm{d}t} = -\lambda N$$

$$\lambda = \frac{\ln 2}{t_{1/2}}$$

$$N = N_0 e^{-\lambda t}$$

$$A = A_0 e^{-\lambda t}$$

## **Gravitational fields**

Gravitational force

$$F = \frac{Gm_1m_2}{r^2}$$

Gravitational field strength

$$g = \frac{Gm}{r^2}$$

Gravitational potential

$$V_{\text{grav}} = \frac{-Gm}{r}$$

#### **Oscillations**

Simple harmonic motion

$$F = -kx$$

$$a = -\omega^2 x$$

$$x = A \cos \omega t$$

$$v = -A\omega \sin \omega t$$

$$a = -A\omega^2 \cos \omega t$$

$$T = \frac{1}{f} = \frac{2\pi}{\alpha}$$

$$\omega = 2\pi f$$

Simple harmonic oscillator

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$



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